

Chapter 3 - Principles of GW Flow

Wells located at $x, y = (0, 0), (15, 20)$ and $(10, 10)$

$$h = 15, 140, 85$$

Assume confined aquifer $\Rightarrow h = Ax + By + C$

$$\text{Well 1} \Rightarrow 15 = 0 + 0 + C \quad \Rightarrow C = 15$$

$$2 \Rightarrow 140 = 15A + 20B + C$$

$$3 \Rightarrow 85 = 10A + 10B + C$$

$$\therefore 15A + 20B = 125 \quad (\text{I})$$

$$10A + 10B = 70 \quad (\text{II})$$

$$2(\text{II}) - (\text{I}) \Rightarrow 5A = 15 \Rightarrow A = 3$$

$$\text{II} \Rightarrow 30 + 10B = 70 \Rightarrow B = 4$$

~~$\therefore h = 3x + 4y + 15$~~

$$\boxed{h = 3x + 4y + 15}$$

\hookrightarrow Check Well 1 $15 = 15 \checkmark$

2 $140 = 45 + 80 + 15$
 $= 140 \checkmark$

3 $85 = 30 + 40 + 15$
 $= 85 \checkmark$

$$\text{Unconfined} \Rightarrow h^2 = Ax + By + C$$

$$\therefore 15^2 = 0 + 0 + C \Rightarrow C = 15^2 = 225$$

$$140^2 = 15A + 20B + C$$

$$85^2 = 10A + 10B + C$$

$$\therefore 15A + 20B = 140^2 - 15^2 \quad (\text{I})$$

$$10A + 10B = 85^2 - 15^2 \quad (\text{II})$$

$$2(\text{II}) - (\text{I}) \Rightarrow 5A = 2(85^2 - 15^2) - (140^2 - 15^2)$$

$$A = -1075$$

$$(\text{II}) \Rightarrow 10B = 85^2 - 15^2 - 10A = 17750$$

$$B = 1775$$

$$\therefore h^2 = -1075x + 1775y + 225$$

$$\text{Check Well 1} \quad 15^2 = 15^2 \quad \checkmark$$

$$2 \quad 140^2 = 15(-1075) + 20(1775) + 225$$

$$19600 = 19600 \quad \checkmark$$

$$3 \quad 85^2 = 10(-1075) + 10(1775) + 225$$

$$7225 = 7225 \quad \checkmark$$