

HW6

① In all instances I still expect incomplete mixing to take
in and result in a late time scaling of $t^{-1/4}$.

What changes is when this happens

- (i) Incomplete mixing happens earlier.
- (ii) " " " even earlier than in (i)
- (iii) " " " earlier (diffusion is less efficient)
- (iv) " " " later (" " more ")
- (v) " " " earlier (reaction is more efficient than mixing)
- (vi) " " " later (reaction is less efficient than mixing)

② This problem is analogous to

$$\frac{\partial c_A}{\partial t} = D \frac{\partial^2 c_A}{\partial x^2} - r$$

$$c_A c_B = 0$$

$$\frac{\partial c_B}{\partial t} = D \frac{\partial^2 c_B}{\partial x^2} - r$$

$$\frac{\partial c_C}{\partial t} = D \frac{\partial^2 c_C}{\partial x^2} + r$$

$$u_A = c_A + c_C \Rightarrow \frac{\partial u_A}{\partial t} = D \frac{\partial^2 u_A}{\partial x^2} \quad u_A(t=0) = \delta(x-5)$$

$$u_B = c_B + c_C \Rightarrow \frac{\partial u_B}{\partial t} = D \frac{\partial^2 u_B}{\partial x^2} \quad u_B(t=0) = \delta(x+5)$$

$$c_C = \min(u_A, u_B)$$

$$M_A = 1 - M_C = 1 - 2 \int_0^{\infty} u_B dx \quad (\text{see HW 4})$$

Due to incomplete mixing your code should predict $M_A \text{ particles} > M_A$.

③ In class we saw
$$\frac{d\langle c_A \rangle}{dt} = -k \langle c_A \rangle^2 - k \langle c_A' c_B' \rangle$$

and argued $\langle c_A' c_B' \rangle$ scales like the peak of the conservative Greens function or $\frac{1}{E}$

where E is dilution index

For pure shear $E \sim t \sqrt{\frac{4\pi \nu t}{3}} \sim t^2$ at late times

∴ Dominant Balance of $k \langle c_A \rangle^2$ and $k \langle c_A' c_B' \rangle$

suggests $\langle c_A \rangle^2 \sim \frac{1}{E} \sim t^{-2}$

⇒ $\langle c_A \rangle \sim t^{-1}$

↓
as if well mixed
even if it is not!